

13.06.2024.



# EXPLORING SUBSTRATE-INDUCED PHASE TRANSITION IN METALLIC CHROMIUM FOIL USING X-RAY ABSORPTION SPECTROSCOPY

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Vitalijs Dimitrijevs, Alexei Kuzmin

[Vitalijs.Dimitrijevs@cfi.lu.lv](mailto:Vitalijs.Dimitrijevs@cfi.lu.lv)



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CIETVIELU FIZIKAS INSTITŪTS  
INSTITUTE OF SOLID STATE PHYSICS  
UNIVERSITY OF LATVIA





# OUTLINE

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## 1. Anisotropy in metals

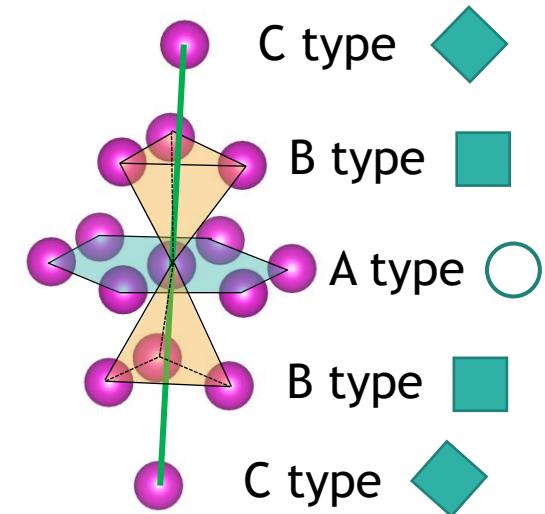
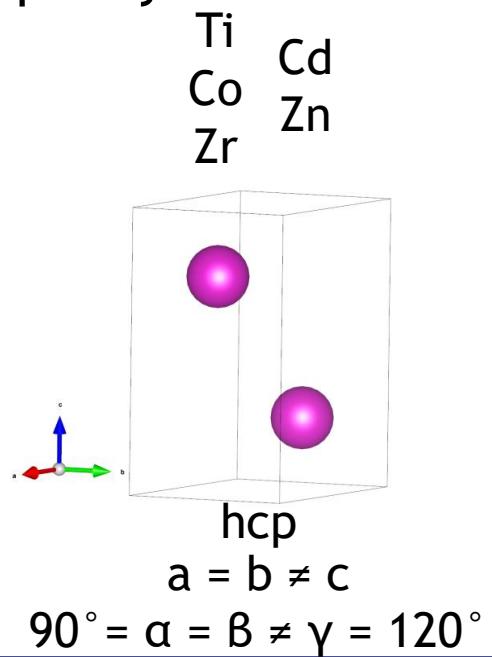
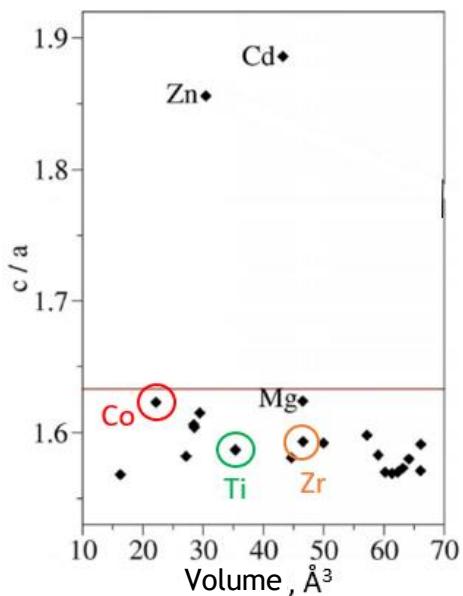
- Samples
- Experiment
- Reverse Monte Carlo Simulations
- Data analysis
- Results

## 2. Thin chromium layer on a substrate

# ANALYZED SAMPLES

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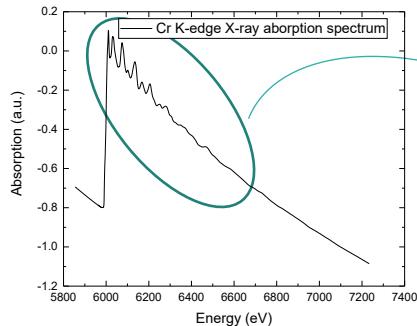
Metallic foils were analyzed: purity 99.2%-99.99%; thickness 4-25 µm



# XAS EXPERIMENT AND OVERALL ANALYSIS ROUTE



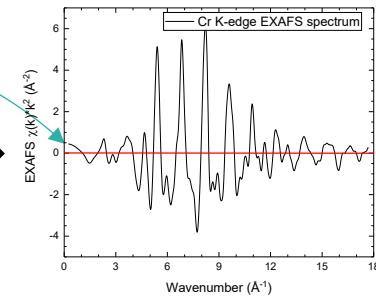
DESY PETRA III P65 Beamline



Mean-square Relative  
Displacements (MSRDs)

Analysis of  
coordinates

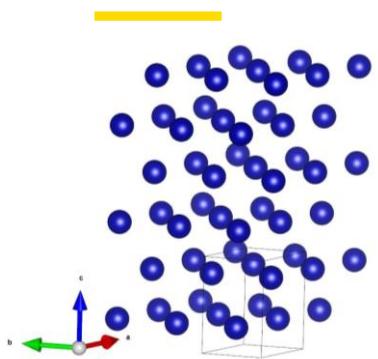
Or  
Analysis of Radial  
Distribution  
Functions (RDF)



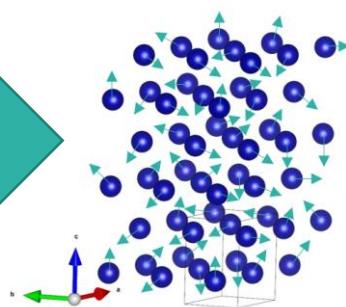
Reverse Monte  
Carlo (RMC)



# DETAILS OF RMC SIMULATIONS

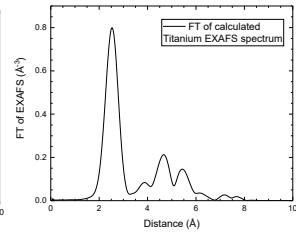
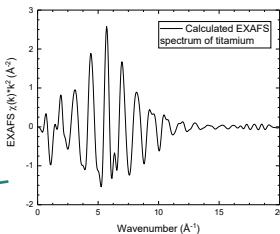


RMC  
(EvAX)



$$\chi(k) = \sum_{i=2}^n \chi_i(k) = \sum_{i=2}^n \sum_j A(k, R_j) \sin(2kR_j + \Phi(k, R_j))$$

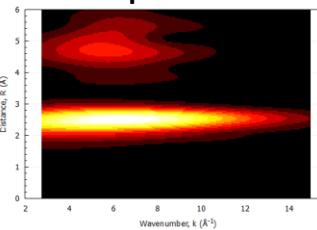
EXAFS calc  
(FEFF 8.5L)



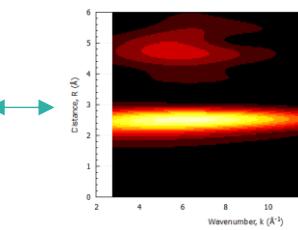
Calculated data

Accept or reject new structure  
+ evolutionary algorithm

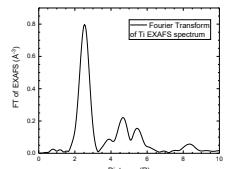
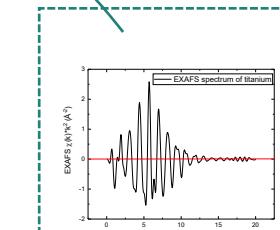
Experiment



Calculations



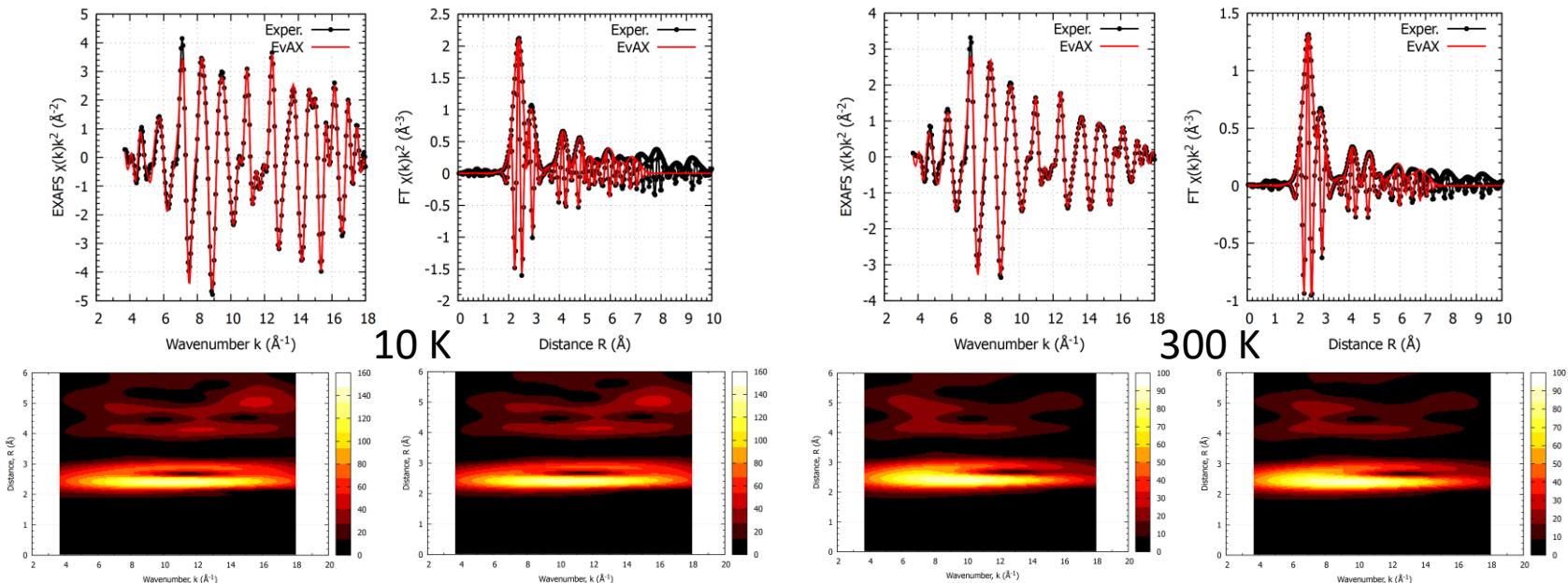
Simultaneously compare in R and k space



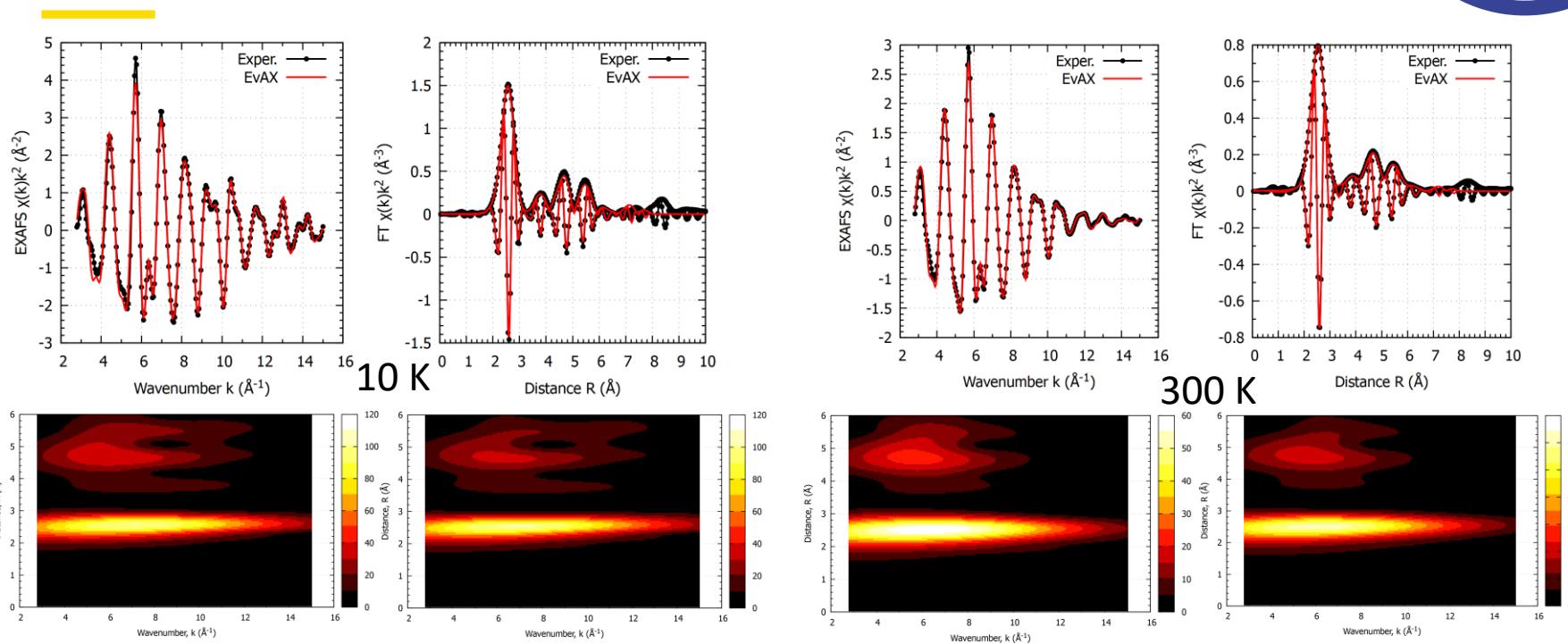
Experimental data



# RMC FIT FOR MOLYBDENUM FOIL (BCC) AT 10 AND 300 K



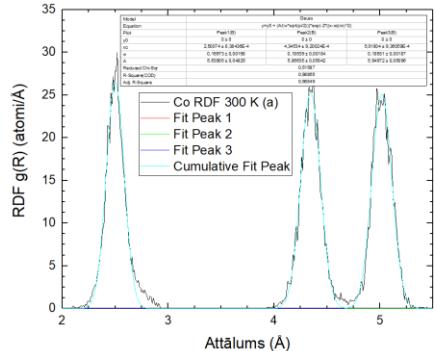
# RMC FIT FOR TITANIUM FOIL (HCP) AT 10 AND 300 K



# DATA ANALYSIS AFTER RMC

1

## Analysis of RDF



$$y = \frac{A}{\sigma\sqrt{2\pi}} e^{-\frac{(x-x_c)^2}{2\sigma^2}}$$

A - number of atoms in a component  
 $x_c$  - interatomic distance  
 $\sigma^2$  - MSRD

## How to define atomic pair types?

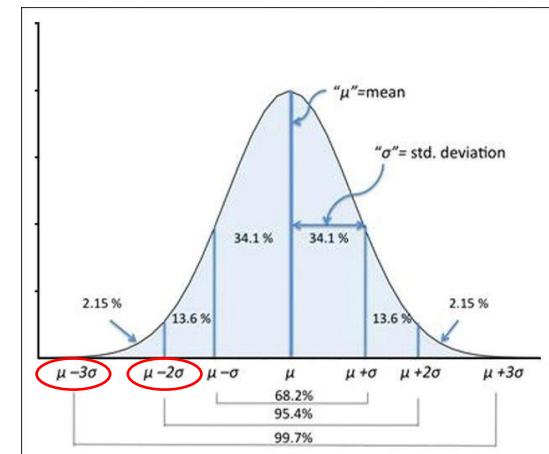
First way:  
From final structure

Second way:  
From equilibrium structure

2

## Analysis of coordinates

$$MSRD = \frac{1}{N} \sum_k (R_k - \bar{R})^2$$





# MSRD DEPENDENCE ON TEMPERATURE FOR Cr-Cr ATOMIC PAIRS (BCC)

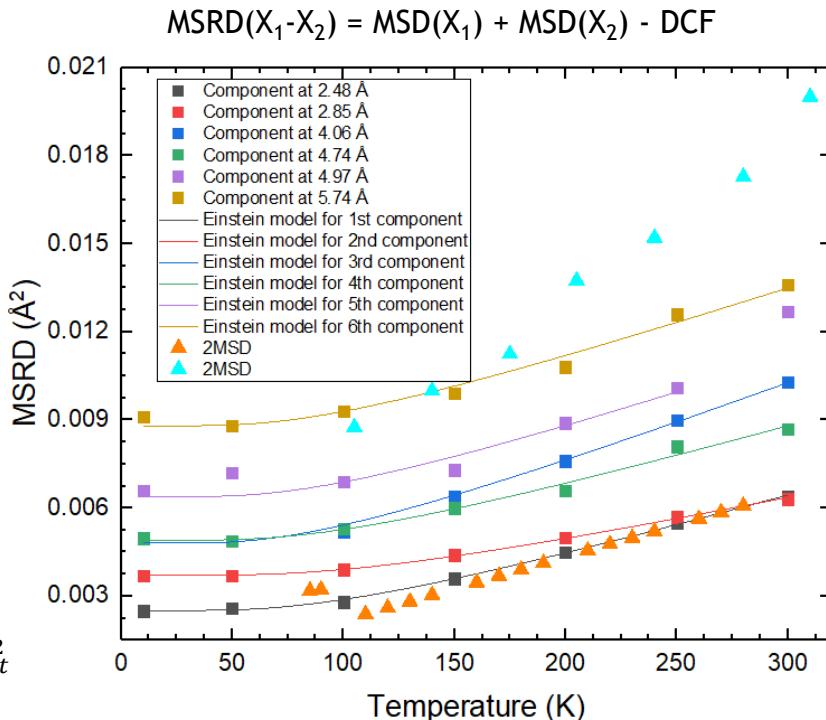
Errors:

x axes  $\pm 2$  K

y axes  $\pm 0.0005 \text{ \AA}^2$

Sample	Distance, Å	Pair type	Force constant, N/m
Bcc Cr	2,48	-	62,4 $\pm$ 0,8
	2,85		84 $\pm$ 1
	4,06		48 $\pm$ 1
	4,74		63 $\pm$ 2
	4,97		54 $\pm$ 4
	5,74		54 $\pm$ 3

$$\sigma^2(T) = \frac{\hbar}{2\mu\omega_E} \coth\left(\frac{\hbar\omega_E}{2k_B T}\right) + \sigma_{st}^2$$



Literature: MSD from phonon density of states

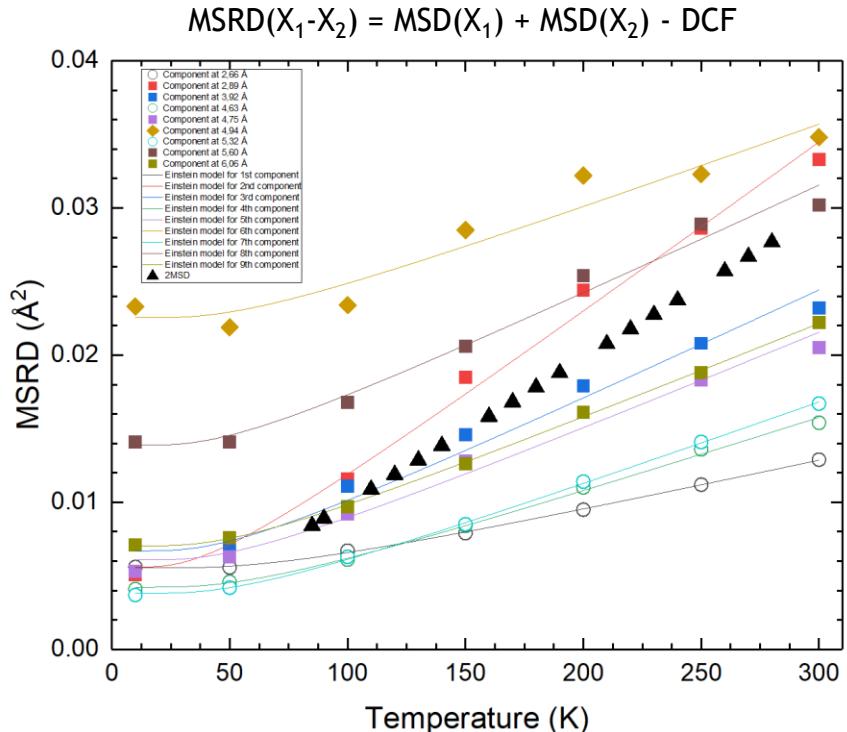
▲ Peng, L.-M.; Ren, G.; Dudarev, S. L.; Whelan, M. J. Debye-Waller Factors and Absorptive Scattering Factors of Elemental Crystals. *Acta Crystallogr. A* **1996**, 52 (3), 456–470.  
<https://doi.org/10.1107/S010876739600089X>

△ Singh, N.; Sharma, P. K. Debye-Waller Factors of Cubic Metals. *Phys. Rev. B* **1971**, 3 (4), 1141–1148.  
[https://doi.org/10.1103/PhysRvB.3.1141.](https://doi.org/10.1103/PhysRvB.3.1141)

# MSRD DEPENDENCE ON TEMPERATURE FOR Zn-Zn ATOMIC PAIRS (HCP)

Sample	Distance, Å	Pair type	Force constant, N/m
Zn	2,66	A	$29,3 \pm 0,4$
	2,89	B	$11,8 \pm 0,4$
	3,62	B	$18,3 \pm 1,1$
	4,63	A	$26,7 \pm 0,5$
	4,75	B	$20,6 \pm 1,1$
	4,94	C	$23 \pm 2$
	5,32	A	$24,1 \pm 0,2$
	5,60	B	$18,4 \pm 1,0$
	6,06	B	$21,1 \pm 0,2$

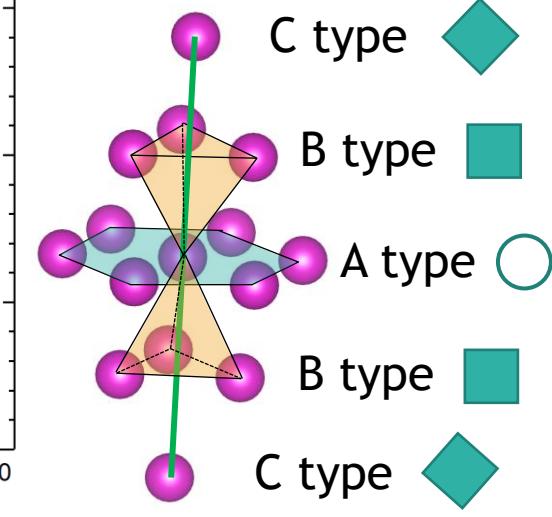
$$\sigma^2(T) = \frac{\hbar}{2\mu\omega_E} \coth\left(\frac{\hbar\omega_E}{2k_B T}\right) + \sigma_{st}^2$$



$$c/a = 1.86$$

$$c/a_i = 1.63$$

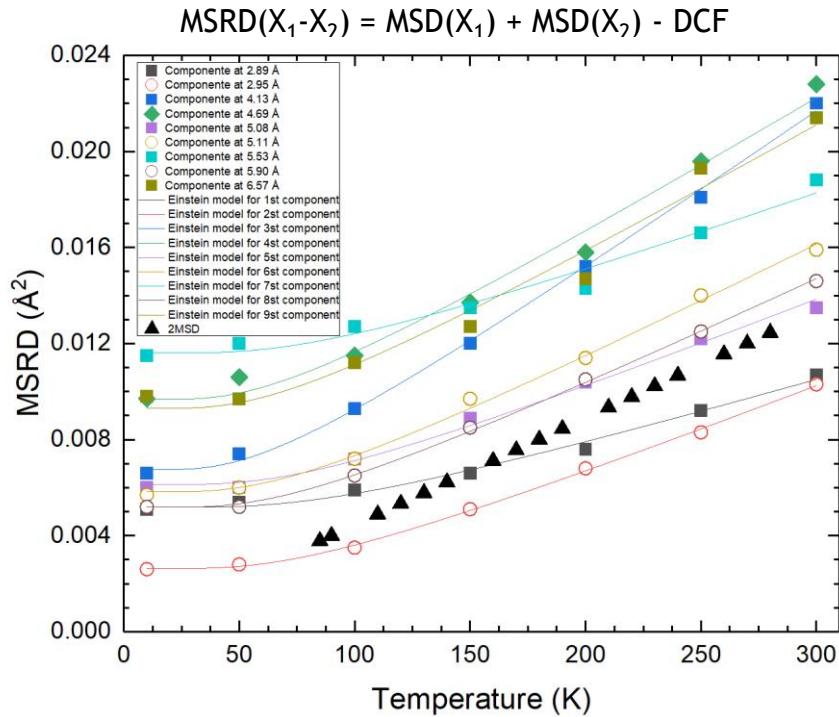
Errors:  
x axes  $\pm 2$  K  
y axes  $\pm 0.002 \text{ Å}^2$



# MSRD DEPENDENCE ON TEMPERATURE FOR Ti-Ti ATOMIC PAIRS (HCP)

Sample	Distance, Å	Pair type	Force constant, N/m
Ti	2,89	B	48,3 ± 1,6
	2,95	A	36,2 ± 0,4
	4,13	B	20,5 ± 0,3
	4,69	C	23,8 ± 1,0
	5,08	B	35,8 ± 1,1
	5,11	A	28,1 ± 0,6
	5,53	B	40 ± 3
	5,90	A	30,0 ± 0,3
	6,57	B	25,1 ± 1,5

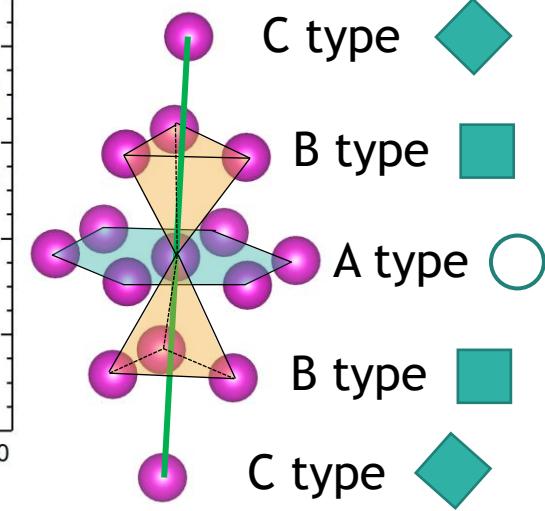
$$\sigma^2(T) = \frac{\hbar}{2\mu\omega_E} \coth\left(\frac{\hbar\omega_E}{2k_B T}\right) + \sigma_{st}^2$$



$$c/a = 1.59$$

$$c/a_i = 1.63$$

Errors:  
x axes ± 2 K  
y axes ± 0.001 Å²

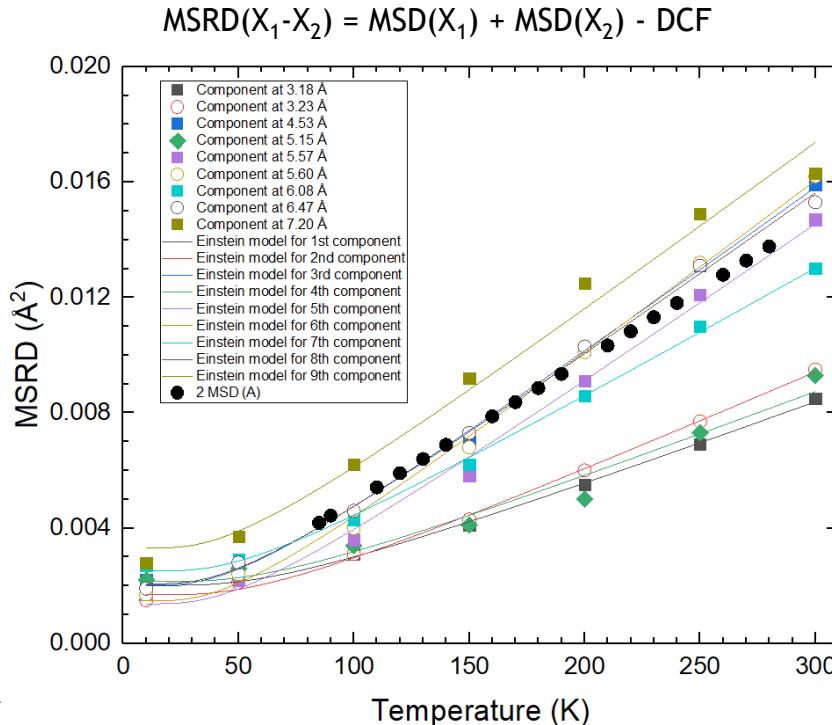


# MSRD DEPENDENCE ON TEMPERATURE FOR Zr-Zr ATOMIC PAIRS (HCP)



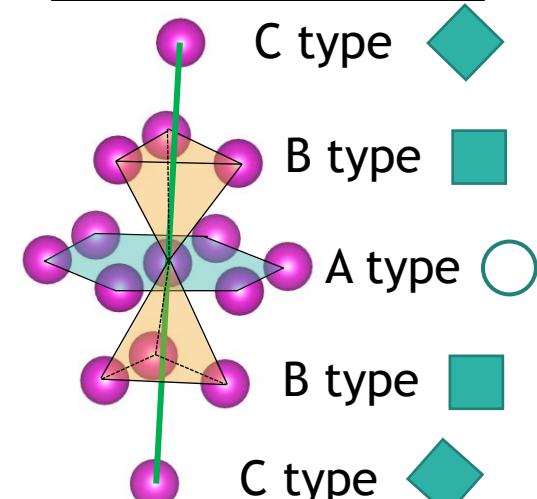
Sample	Distance, Å	Pair type	Force constant, N/m
Zr	3,18	B	46,7 ± 0,7
	3,23	A	39,5 ± 0,8
	4,53	B	23,7 ± 0,4
	5,15	C	45 ± 3
	5,57	B	24,7 ± 0,8
	5,60	A	22,6 ± 0,5
	6,08	B	30,2 ± 0,5
	6,47	A	24,1 ± 0,4
	7,20	B	23,3 ± 1,2

$$\sigma^2(T) = \frac{\hbar}{2\mu\omega_E} \coth\left(\frac{\hbar\omega_E}{2k_B T}\right) + \sigma_{st}^2$$



$$\begin{aligned} c/a &= 1.59 \\ c/a_i &= 1.63 \end{aligned}$$

Errors:  
x axes ± 2 K  
y axes ± 0.002 Å²





# CONCLUSION ABOUT FIRST PART

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- The use of partial Radial Distribution Functions (RDF) enabled the analysis of overlapping components, corresponding to various atomic pair types
- The anisotropy of local lattice dynamics in hcp metals is influenced by c/a ratio and can be observed from MSRD dependence on temperature



# THIN CHROMIUM LAYER ON A SUBSTRATE

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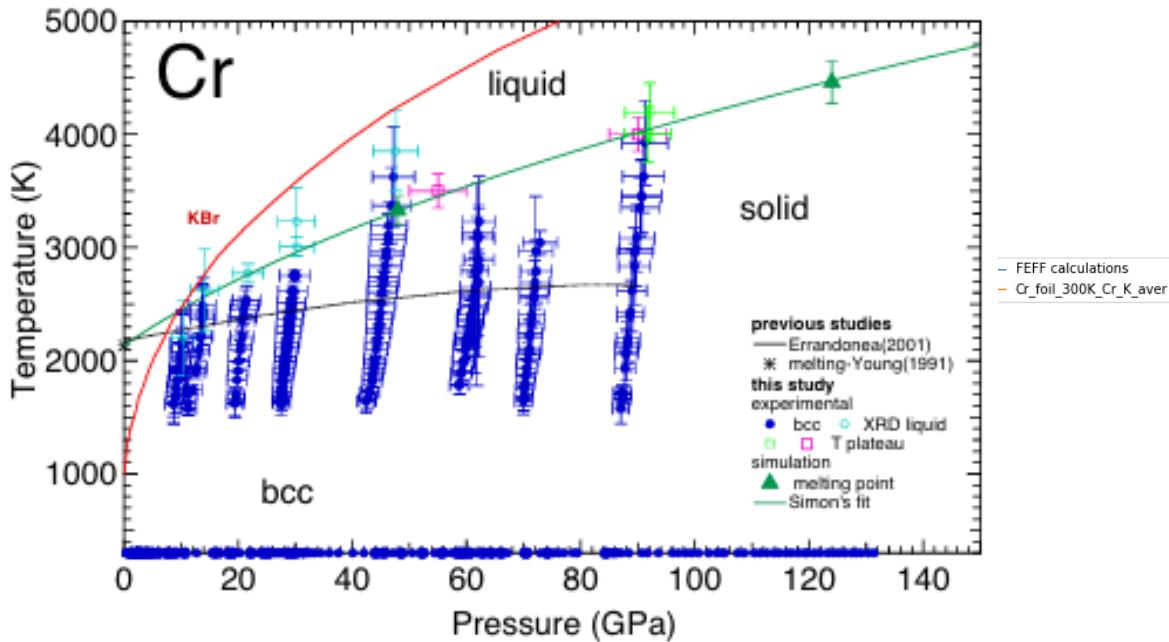
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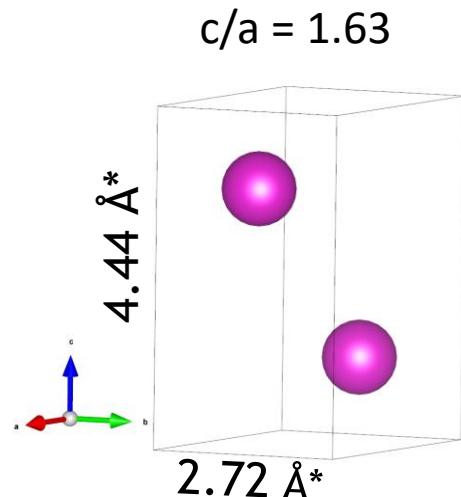
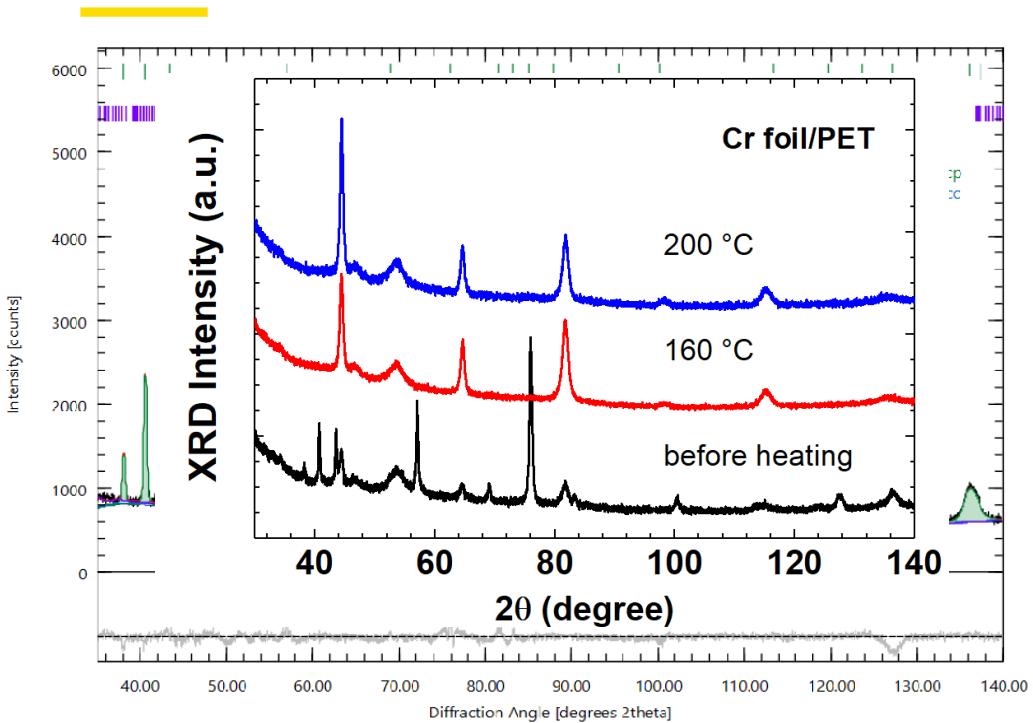
# NOTHING WAS WRONG UNTIL...

Cr 2 µm + 125 µm  
Polyester substrate



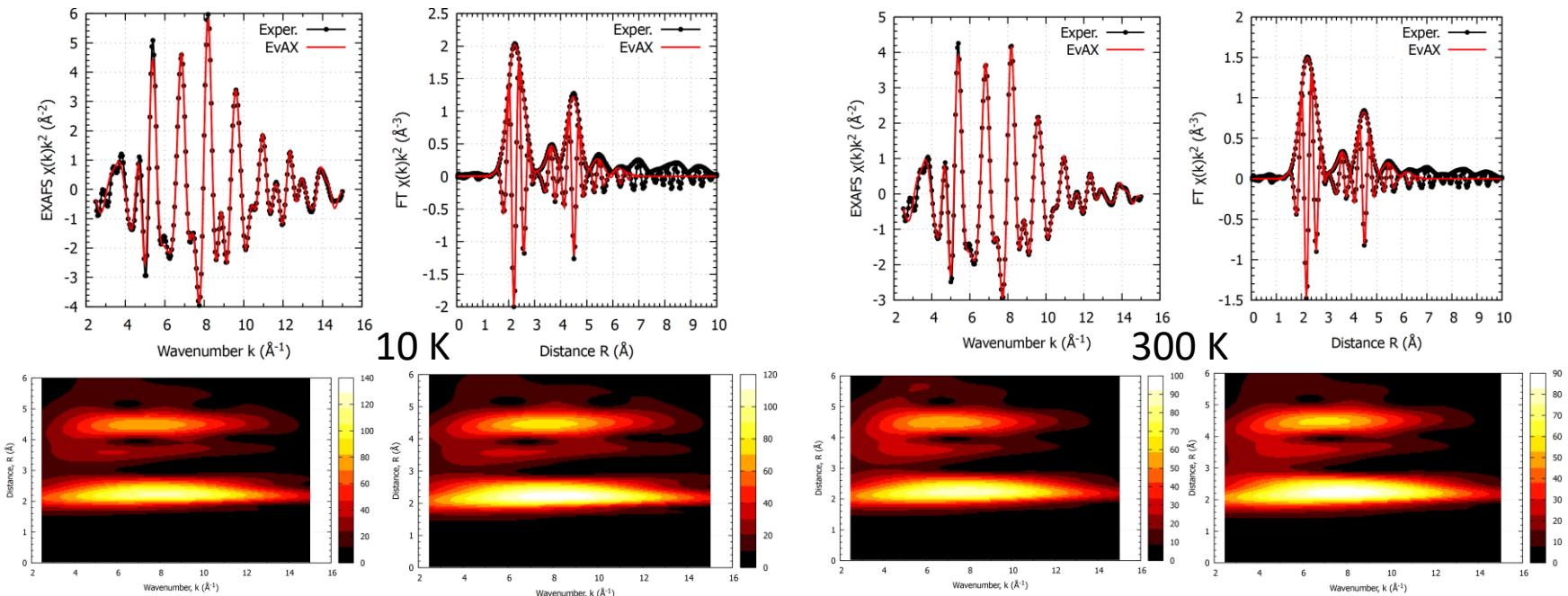


# XRD ANALYSIS BY RIETVELD REFINEMENT

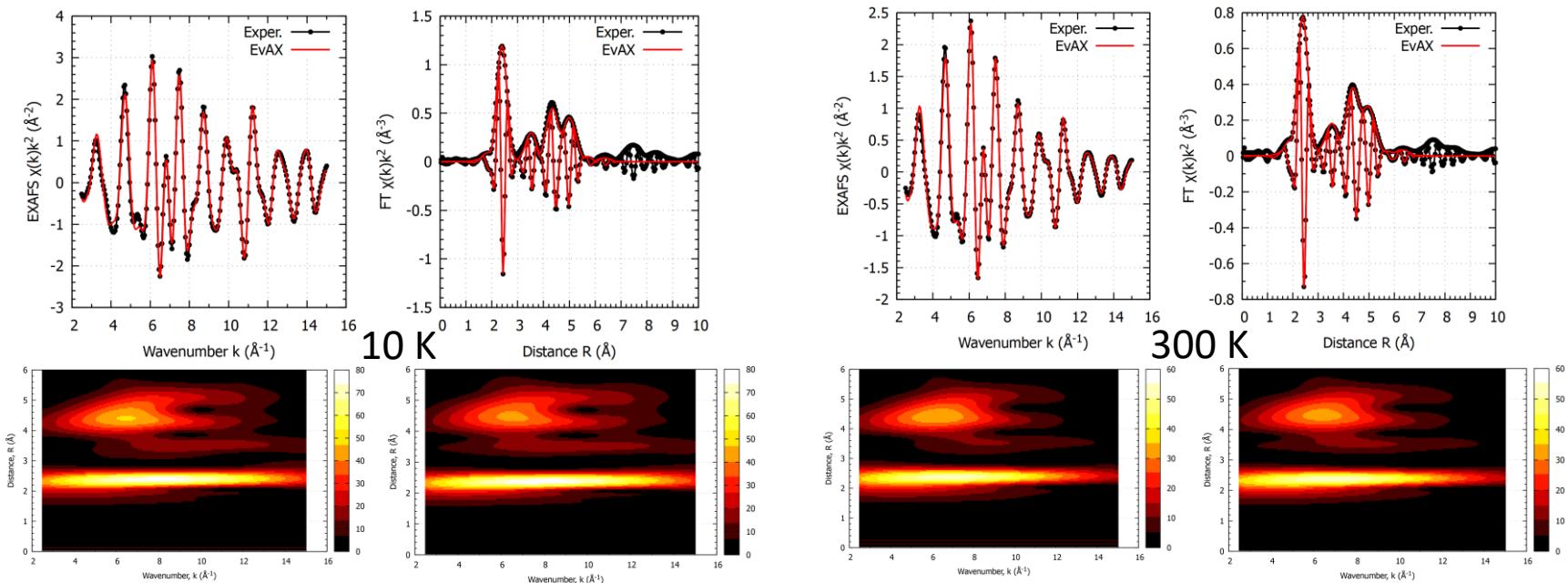


\*Rounded data  
Error  $\pm 0.00001$

# RMC FIT FOR CHROMIUM FOIL (BCC) AT 10 AND 300 K



# RMC FIT FOR CHROMIUM FOIL (HCP) AT 10 AND 300 K

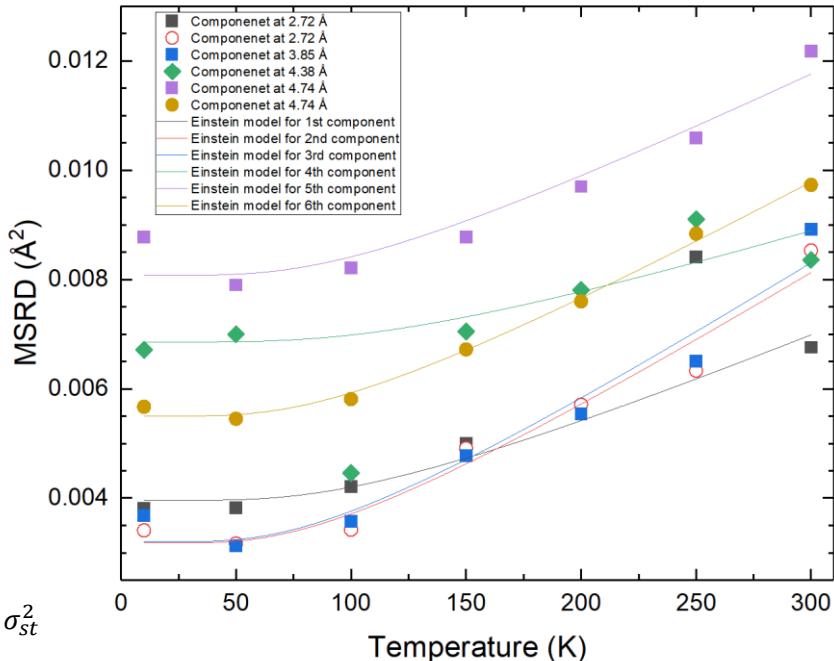


# MSRD DEPENDENCE ON TEMPERATURE FOR Cr-Cr ATOMIC PAIRS (HCP)



$$\text{MSRD}(X_1-X_2) = \text{MSD}(X_1) + \text{MSD}(X_2) - \text{DCF}$$

Sample	Distance, Å	Pair type	Force constant, N/m
Hcp Cr	2,72	B	$53 \pm 2$
	2,72	A	$69 \pm 7$
	3,85	B	$53 \pm 2$
	4,38	C	$34 \pm 5$
	4,74	B	$64 \pm 7$
	4,74	A	$70 \pm 3$

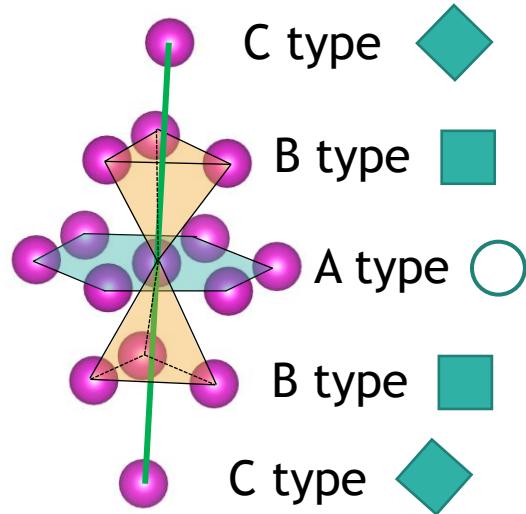


$$\sigma^2(T) = \frac{\hbar}{2\mu\omega_E} \coth\left(\frac{\hbar\omega_E}{2k_B T}\right) + \sigma_{st}^2$$

$$c/a = 1.63$$

$$c/a_i = 1.63$$

Errors:  
x axes  $\pm 2$  K  
y axes  $\pm 0.002 \text{ \AA}^2$





## CONCLUSIONS FROM SECOND PART

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- Substrate-induced phase transition from bcc to hcp phase was detected in thin chromium foil on polyester substrate. This effect is analogous to that produced by the application of negative pressure
- Contrary to the anisotropic local lattice dynamics typically observed in hexagonal close-packed metals, hcp chromium exhibits isotropic behavior



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# THANKS FOR YOUR ATTENTION!



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The financial support from the Latvian Council of Science project No. Izp-2022/1-0608 is greatly acknowledged.